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Antenna Laboratory

Technical Report No. 55

AN INVESTIGATION OF THE NEAR FIELDS ON THE CONICAL
EQUIANGULAR SPIRAL ANTENNA

by

O. L. McClelland

Contract AF33(657)-8460

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ABSTRACT

The current distribution has been measured on a conical equiangular spiral antenna. A correlation between the operation of the conical log-spiral antenna and the operation of the uniform circular bifilar helix is established by utilizing a general theory of backward wave radiation from periodic structures. Operation beyond the normal frequency limits has been explored and discussed. The arms of the antenna were constant diameter conductors. The effects of this deviation from the ideal design, which calls for a linearly increasing diameter, have been observed. The far field measurements, giving for example the center of phase location, agrees with the near field probing.

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1. INTRODUCTION

The introduction in 1954 of the concept of frequency independent antennas led to an important breakthrough in the antenna field¹. Many versions of these antennas have been studied since that time. Of these, possibly the two most practical versions from simplicity of construction are the log-periodic dipole array^{2,3} and the wire-arm version of the conical log-spiral⁴.

In an effort to provide information that would lead to a better understanding of the operation of the conical log-spiral antenna, an experimental investigation was made of the amplitude and phase of the near fields on one antenna. The purpose of this paper is to present this data and to indicate how it correlates with a general theory of backward wave radiation from periodic structures⁵.

2. THE BASIC ANTENNA

The conical log-spiral antenna with its associated coordinate system is shown in Figure 1. Only the center line of the antenna arm has been shown because the antenna dealt with here was the constant width arm version of the conical log-spiral antenna. If one looks at the triangle formed by $a d\varphi$, $d\rho$ and ds where a is the radius of the cone at the element of circumference $a d\varphi$, $d\rho$ is an element of the radius vector, and ds is an element of arm length, it will be seen that

$$\tan \alpha = \frac{a d\varphi}{d\rho}$$

but

$$a = \rho \sin \theta_0$$

where θ_0 is the half angle of the cone and therefore

$$\frac{d\rho}{\rho} = \frac{\sin \theta_0}{\tan \alpha} d\varphi$$

giving the equation for the equiangular curve

$$\rho = \rho_0 \exp \left(\frac{\sin \theta_0}{\tan \alpha} \varphi \right)$$

where ρ_0 is a constant factor arising from the tip truncation.

Again looking at the same triangle, it is observed that

$$d\rho = \cos \alpha \, ds$$

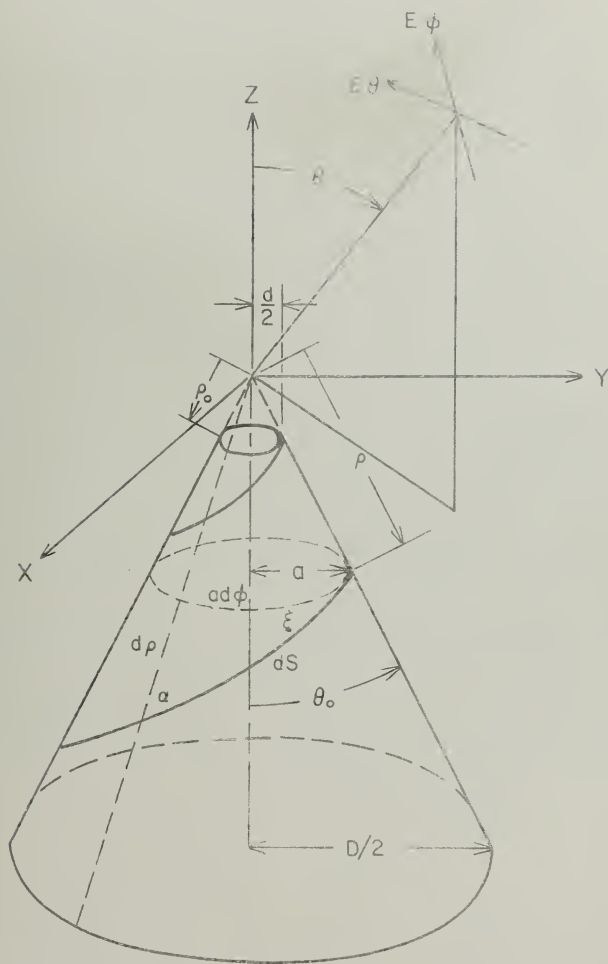


Figure 1. A conical log-spiral antenna with its associated coordinate system

or

$$\rho = S \cos \alpha + \text{constant}$$

In the case where there is no truncation, i.e., when $S = 0$ for $\rho = 0$, the constant is zero yielding

$$\rho = S \cos \alpha$$

If the cone has been truncated, $S = 0$ but $\rho = \rho_0$. Then the constant $= \rho_0$ and

$$\rho = S \cos \alpha + \rho_0$$

It will be convenient later to speak in terms of pitch angle as commonly defined for the cylindrical helix. The pitch angle ξ is the complement of the constant spiral angle α which the curve makes with a radius vector of the cone. To summarize the results and add a few obvious relationships, we have

In terms of spiral angle α

$$\rho = \rho_0 \exp \left[\frac{\sin \theta_0}{\tan \alpha} \varphi \right]$$

$$\rho = S \cos \alpha$$

In terms of pitch angle ξ

$$\rho = \rho_0 \exp [(\sin \theta_0 \tan \xi) \varphi]$$

$$\rho = S \sin \xi$$

and for both cases

$$a = \rho \sin \theta_0$$

$$d = 2 \rho_0 \sin \theta_0$$

$$D = \rho_{\max} \sin \theta_0$$

$$C = 2\pi a$$

3. BACKWARD WAVE RADIATION FROM THE CONICAL LOG-SPIRAL

In the spring of 1961 Mayes, Deschamps, and Patton⁵ indicated that frequency independent antennas could be analyzed by considering them to be locally periodic structures whose period varies slowly, increasing with distance from the apex. At any given frequency there is a region on the spiral where the current is phased properly to produce radiation toward the apex and hence produce backward wave radiation. It was postulated that this region on the conical log-spiral antenna could be approximated by a bifilar helix with parameters equal to the average conical spiral parameters over this region.

In an effort to apply this idea to the conical antenna, it is instructive to consider some of the techniques which have been useful in the analysis of helices. The Brillouin diagram, relating the propagation constant h on the surface of the helix to the frequency ω or to $k = \omega/c$ the propagation constant in free space, has been a convenient tool in the analysis of periodic structures and in particular the helix⁶.

In the derivation of the Brillouin or k - β for the helix, it has been shown^{7,8} that h is real in the regions defined by the boundaries

$$m + \frac{ka}{\cot \xi} < \frac{|h|a}{\cot \xi} < m - \frac{ka}{\cot \xi} ;$$

m is a positive real integer. A consequence of this is that for h to be real $ka/\cot \xi \leq 1$ for the bifilar helix. The unshaded areas in Figure 2 designate the regions where h is real. Sensiper⁷ has shown that the solutions of the determinantal equation can be approximated by the line $ka/\cot \xi = ha/\cot \xi \sin \xi$, which can be interpreted as a wave progressing at the speed of light

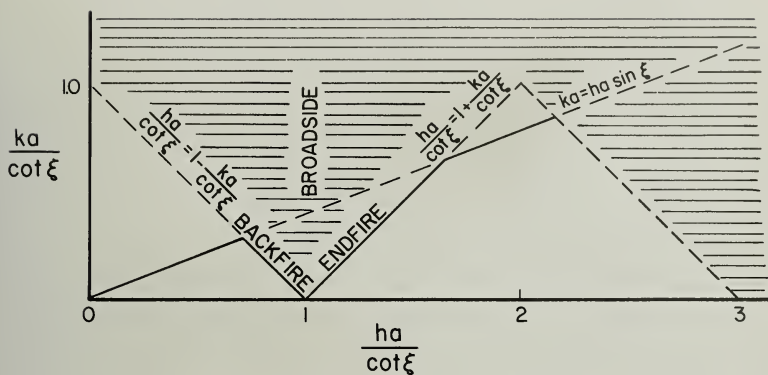


Figure 2a. Typical k - β diagram for bifilar helix when considering operation along the cylinder surface

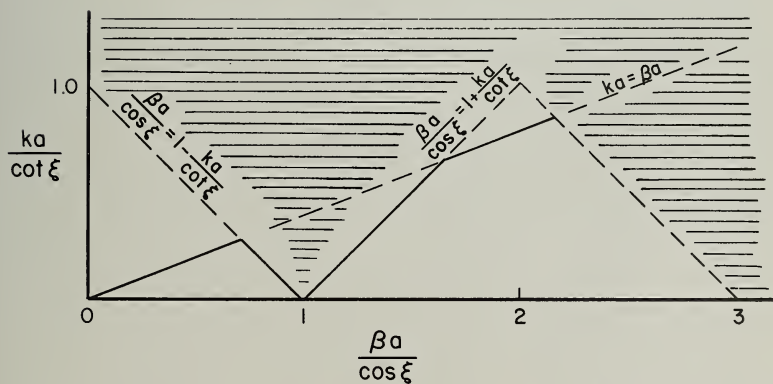


Figure 2b. Typical k - β diagram for bifilar helix when considering operation along the conductor

along the thin tape, and the $m=1$ boundaries of the regions discussed above are shown in Figure 2a. As Sensiper has indicated, for many practical purposes, these roots are the only ones which may need to be considered on the cylinder surface. It was felt, since the data were taken along the conductor, that a $k-\beta$ diagram as shown in Figure 2b was more applicable for this presentation. This diagram is essentially the same as Figure 2a, where $\beta = h \sin \xi$, the propagation constant along the conductor is used as the variable. It should be noted here that the relation shown in this diagram should be applicable only to an infinite, thin-tape helix. When the tape is not thin, the current progression will deviate from the speed of light. It has been demonstrated, however, that experimental data taken on a finite helix agrees quite well with the diagram⁷.

The locus of the propagation constant in Figure 2b will give a value of βa real for each value of ka . In the case of the helix, the radius a and pitch angle ξ are constants. As the frequency is increased, the value of β scans as the diagram predicts. In the case of the log-spiral, the pitch angle ξ is constant, but the radius a increases linearly with distance from the tip. Since β is a function of a at any particular frequency, β changes with distance from the apex.

4. PHYSICAL CONSTRUCTION CONSIDERATIONS

Two antennas were constructed, one model to operate from approximately 150 mc to 700 mc, and a smaller model with the same tip diameter and construction but with a base diameter just one-half the size of the large model. Therefore, the smaller model had a frequency range from approximately 300 mc to 700 mc. This particular frequency range was chosen to insure that the probing system used during the near field measurements would be small with respect to the wavelength. Most of the data were taken on the small model. Near field measurements were made on the large model in order to observe the effects of the base truncation and to observe a lower frequency of operation. The spiral angle α and one-half the enclosed cone angle θ_0 were selected to insure a small back lobe on the antenna⁴. One-half inch copper tubing was chosen as the constant width arm for ease of construction and probe mounting. The physical dimensions of these antennas are given in Figure 3.

The two copper arms were fed by the infinite balun method, i.e., by inserting a coaxial cable inside one arm with its outer conductor bound to the "feed arm" and its center conductor connected to the "dummy arm" as shown in Figure 5. This gives an anti-symmetric, slit-generator feed which should be as frequency independent as the antenna itself. The bullet-shaped end on the dummy arm was selected for optimum impedance characteristics.

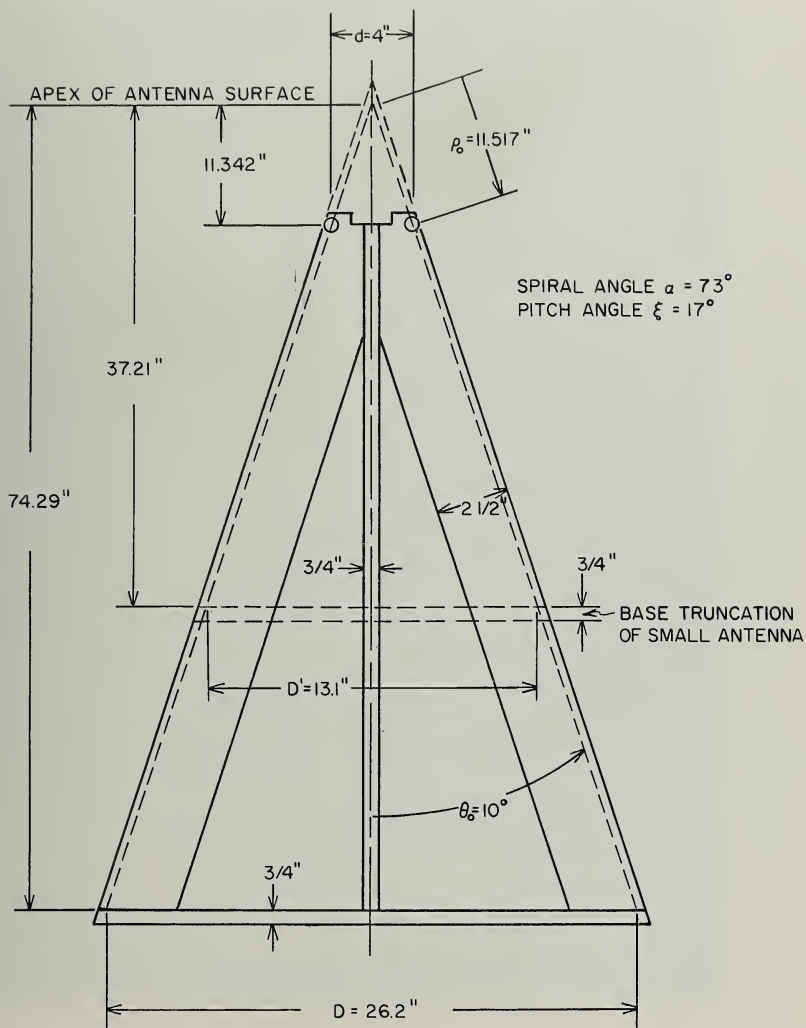


Figure 3. Physical dimensions of the test antennas

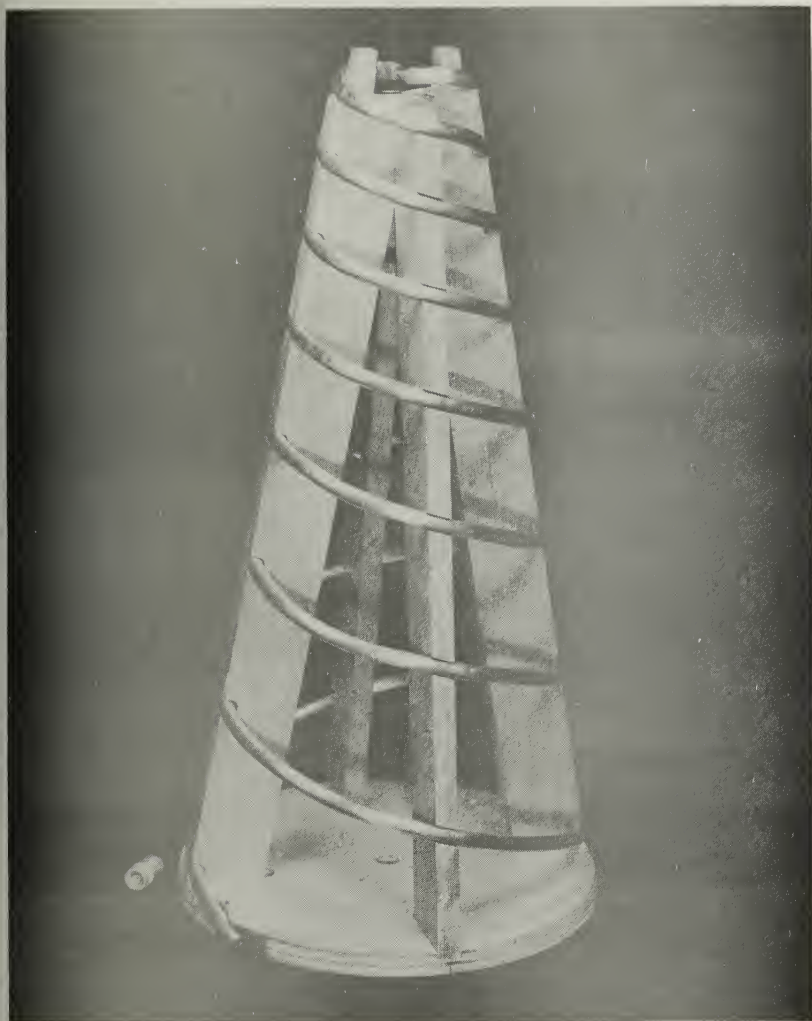


Figure 4. Photograph of the small test antenna

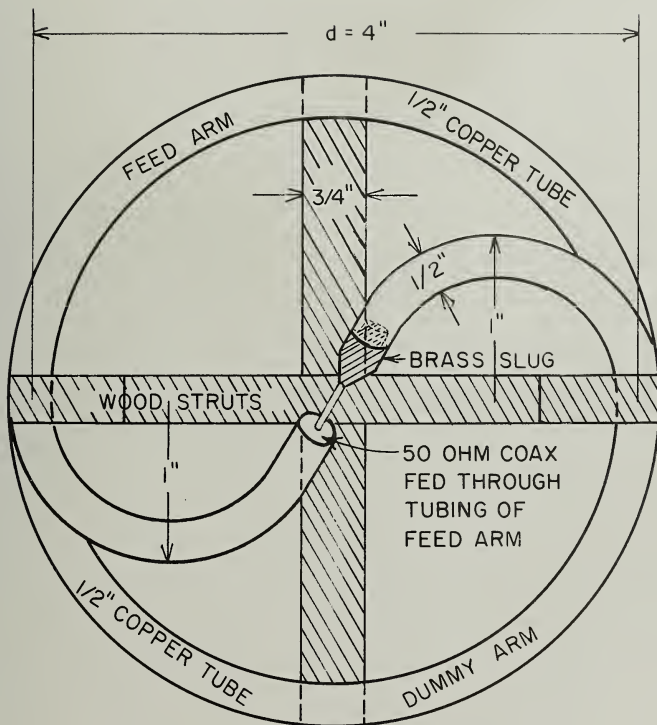


Figure 5. The feed region of the test antenna

5. MEASUREMENT CONSIDERATIONS

Throughout the entire experimental program no attempt was made to prove that the wire version of the conical log-spiral antenna was a "frequency independent" antenna since Dyson⁴ has already established this fact. A definition of frequency independence is given by R. L. Carrel. "By frequency independence as applied to an antenna, it is meant that the observable characteristics of the antenna such as the field pattern and input impedance vary negligibly over a band of frequencies within the design limits of the antenna, and that this band may be made arbitrarily wide merely by properly extending the geometry of the antenna structure. The ultimate band limits of a given design are determined by non-electrical restrictions: size governs the low frequency limit, and precision of construction governs the high frequency limit."³ The antenna was designed to have essentially constant impedance and patterns over a two to one band. Measurements were made over a four to one band in order to investigate the operation beyond the normal limits.

The near field measurements consisted of measuring the relative amplitude and relative phase of the current flowing along the conductor of the antenna. A signal proportional to this current was received from a small shielded current loop probe⁹ shown in Figure 6. The loop probe was placed on the end of a sufficiently long piece of .050 inch microdot cable which was allowed to follow the surface of the antenna arm. The loop itself was mounted on a beryllium copper clip which provided a means of fastening the probe to the one-half inch copper tube arms of the antenna. Calibrated positions were inscribed on the arms to facilitate accurate positioning of the probe.

It was necessary to determine if the presence of the microdot cable was

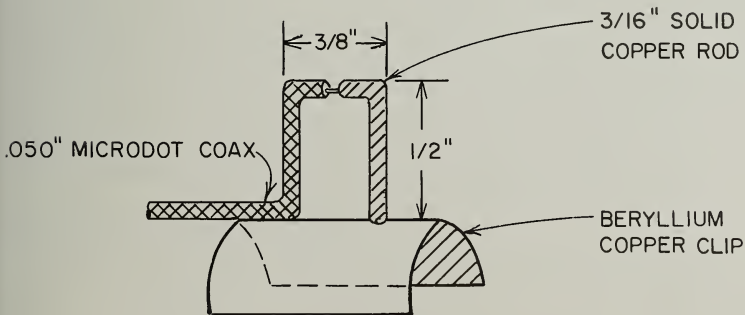
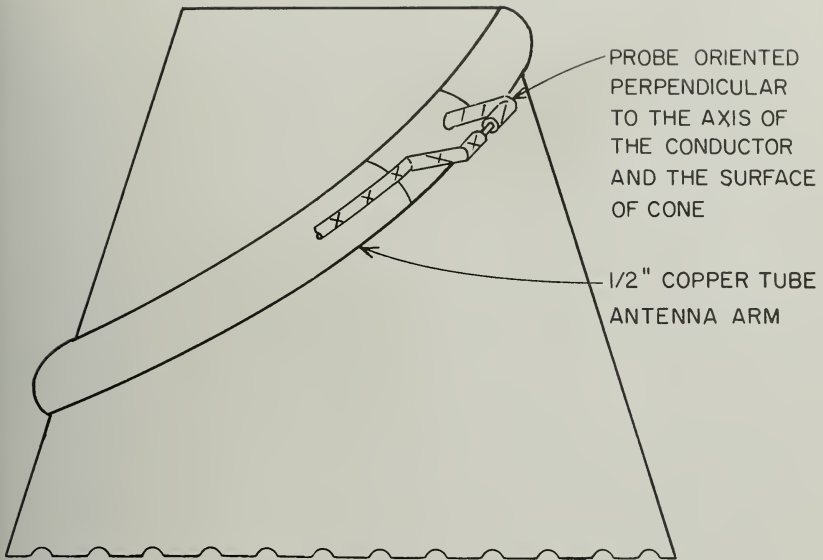


Figure 6. Detail of the probe used for the near field measurements

disturbing the near fields on the antenna arms. Only negligible deviations in the signal level could be determined when a piece of microdot cable was placed in various locations on the arm around the loop. Also, no deviation occurred when an additional shield was placed around the microdot cable indicating negligible leakage from the cable. All data was recorded relative to the same initial position on the antenna arm. No attempt was made to approach the slit-generator feed beyond the point where the antenna arm left the true equiangular curve. Data was taken at approximately 0.1λ intervals along the arm progressing down the antenna. To minimize flexing, the microdot cable was allowed to droop down in a large loop.

5.1 Relative Amplitude Measurements

A block diagram of the circuit used for the amplitude measurements is shown in Figure 7. The output of the RF power oscillator, delivering a continuous wave, was padded and filtered before delivery to the antenna. Two signal taps were provided to allow both frequency and amplitude monitoring. The stubs were tuned to a maximum probe signal level when the probe was placed in the reference position discussed previously. The addition of the 100 mc low pass filter was found to be necessary since the filter provided in the crystal mixer was not adequate to block the RF signal from passing through the mixer to the 30 mc IF amplifier. It was found that a power output of several watts was needed in order to achieve an adequate dynamic range.

5.2 Relative Phase Measurements

The relative phase measuring circuit is diagrammed in Figure 8. The input system to the antenna was similar to the system used for magnitude measurements except the power was not monitored. If the power had drifted, both the reference signal level and the probe signal level would have drifted together and would

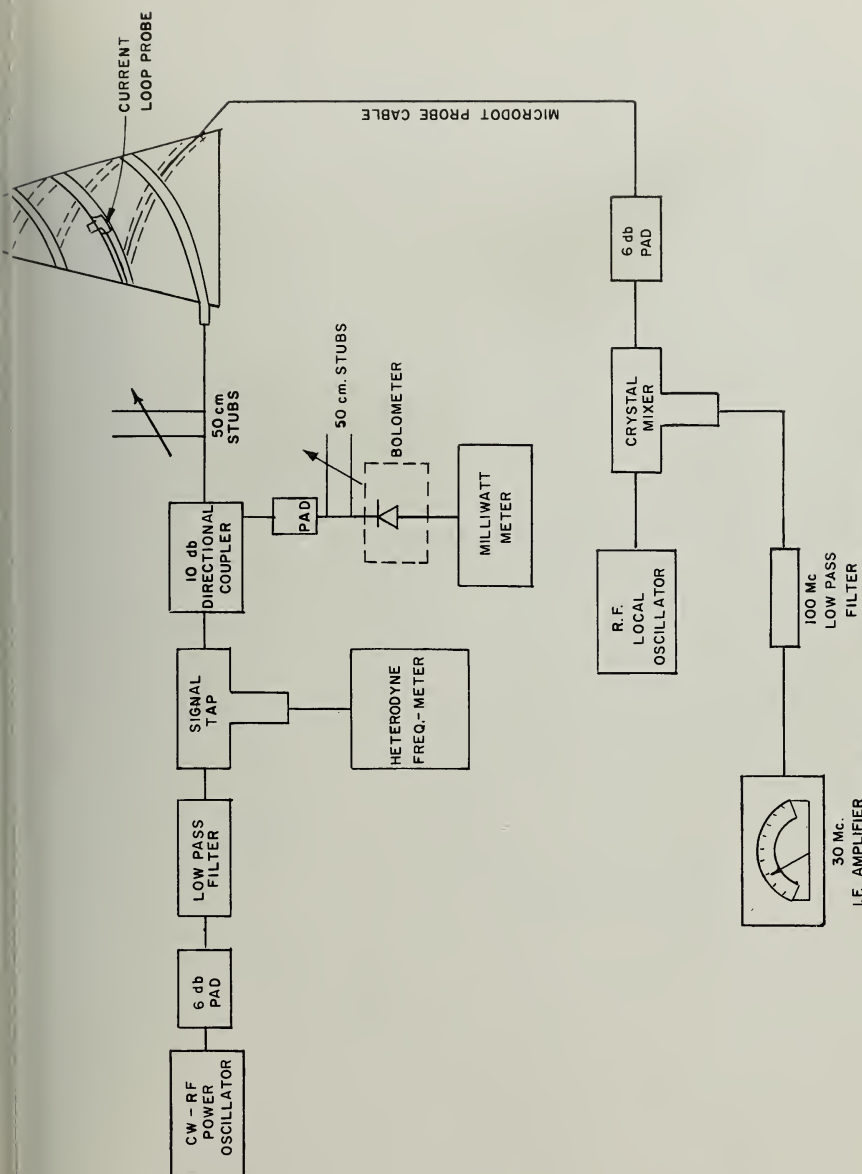


Figure 7. Block diagram of the amplitude measuring circuit

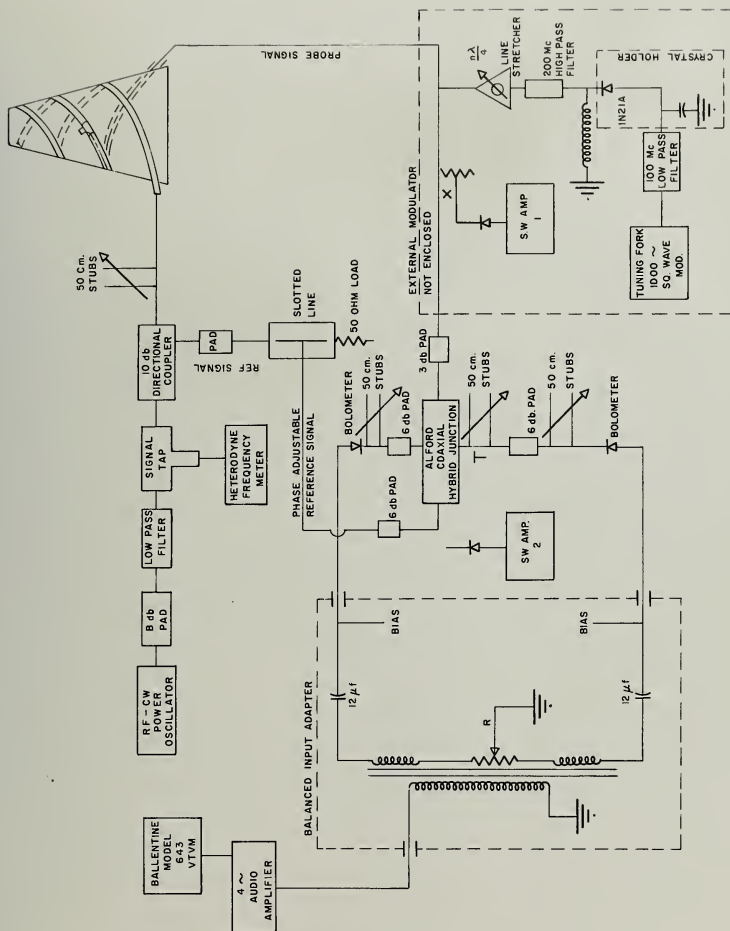


Figure 8. Block diagram of the phase measuring circuit

not have disturbed the measurement.

The theory of the measurement was as follows. The probe signal was externally modulated and fed into either the series or shunt arm of the coaxial hybrid junction. Likewise, the CW reference signal, the phase of which could be adjusted by means of a matched slotted line, was inserted into the remaining shunt or series arm of the hybrid. The outputs of the hybrid, one of the RF phasor sum and the other the RF phasor difference, were independently matched and detected. The two detected audio signals, one the magnitude of the sum, and the other the magnitude of the difference, were subtracted in the balanced input adapter. The difference of these two magnitudes was applied to the audio amplifier and read out on the Ballentine VTVM

As can be seen by the phasor relationships in Figure 9, a sharp null should be observed when the two input signals are in phase quadrature. The phase measurement was somewhat insensitive to the difference in amplitude between the two input signals. A precise null was always present, no matter how large the difference in the amplitudes. Of course, keeping the null above noise was a problem when either the two signals were both small or the difference was great. In either case, the entire standing wave could have been engulfed in the noise. For these particular measurements it was found that the null position could be located with a reasonable degree of accuracy when the relative difference between the probe signal and the reference signal increased to 25 db.

In this measurement, only the probe signal was modulated to provide a sharper null at R. The only error due to the unmodulated reference signal was a leakage through the hybrid junction. Even though the unmodulated signal,

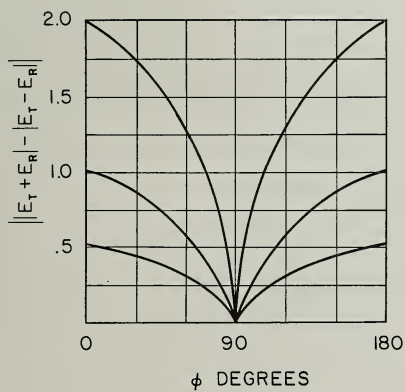
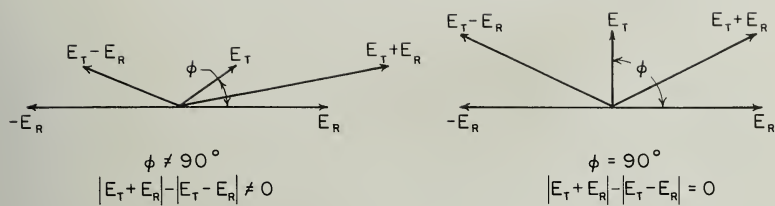


Figure 9. Balanced detection phase measuring system nulls and phasor relationships

which at times was much larger than the modulated probe signal, was present at the detectors, only a DC component was present at the transformer. In a well balanced system the isolation between inputs is in the order of 60 to 70 db.

The following procedure was used to balance the hybrid junction after each change in frequency. Refer again to Figure 8. The external modulator was applied to a signal taken from the 10 db directional coupler. This modulated signal was used throughout the balance procedure. This method was used, as opposed to modulating the source, in order that the frequency used during the balancing procedure would be the same as the frequency used during the phase measurement. Modulation applied directly to the source will shift the frequency. The line stretcher in the modulator was adjusted for maximum deflection on SW amplifier No. 1. At this maximum the distance from the crystal to the probe line was some multiple of a quarter wavelength allowing an optimum switching action to be applied to the RF signal. The hybrid junction and the stubs T were removed from the circuit. Each arm, attached to the outputs of the hybrid, was balanced individually. The modulated signal was applied to one of the detection arms with the resistor R placed for maximum signal observed on the Ballentine VTVM. The stubs in the detection arms were also adjusted for a maximum on this meter. The same procedure was carried out on the other detection arm. In this particular circuit the difference in detected signal from the two arms was less than 0.5 db.

The balanced arms were connected to the hybrid junction and the stubs T. The modulated signal was then increased in amplitude and applied to one input of the hybrid through a 6 db pad. The other input was monitored with SW amplifier No. 2 through a detector and a 6 db pad. The stubs were then adjusted

for a minimum on this meter which was measuring directly any leakage through the hybrid due to unbalance on the output arms. When a minimum was observed, the stubs T were in such a position as to have balanced out any difference in impedance seen by the two output arms. The previous step only insured that the sensitivity of both detectors was the same and did not insure balanced input impedances. Next, the output, which was monitored, was then terminated in a matched load. The resistance R was adjusted for a minimum deflection on the Ballentine VTVM. These last two steps were repeated to insure the highest degree of balance. This completed the balancing procedure and the circuit in Figure 8 was then reassembled and ready for measurements.

The system was checked by two methods. The first was to measure a known phase shift and the second to observe distances between null positions. The first check was performed on the system by measuring a calibrated delay line which was inserted into the probe line. The balancing procedure was continued until the error in measuring the delay line was less than one percent. The maximum error measured after a set of data was taken was less than two percent. The increase in error was accountable to a drift in frequency during the measurement on the antenna. The second check depends upon the fact that if the hybrid junction was perfectly balanced, the distance between consecutive null points would be one-half of one free-space wavelength. Therefore, during the measurement, the distances between nulls were tabulated and compared as the phase was shifted and successive nulls were followed. If the distance between nulls began to deviate, one from another, it was an indication that the hybrid was becoming unbalanced. If the hybrid was unbalanced, the sum of the distances among three consecutive nulls was equal to a free-space wavelength; but the distance between two consecutive nulls was not one-half of one free-space wavelength.

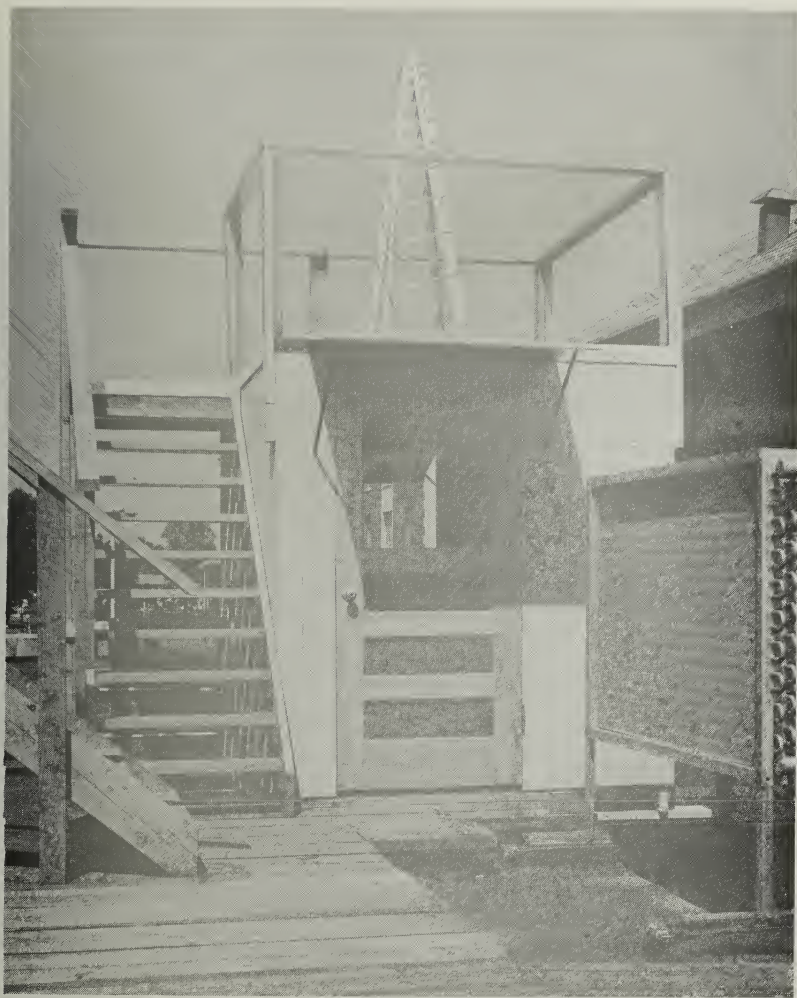


Figure 10. Photograph of the large antenna mounted in the measurement site

6. EXPERIMENTAL RESULTS

6.1 The Current Distribution

The relative magnitude of the current distribution has been measured at six frequencies, from 300 mc to 800 mc, on the small model and at four frequencies, from 200 mc to 800 mc, on the large model. The relative phase of the current was measured at five frequencies from 400 mc to 800 mc on the small model only. This data is displayed in Figures 11 through 23 inclusive.

Figures 11 through 17 indicate two items of interest:

(1) A rapid decay in the amplitude over the first portion of the structure. The rate of decay over this first portion tended to be frequency dependent, i.e., increasing rate with increasing frequency. This indicated that the rate of decay was a function of arm width in wavelengths as was noted by Dyson¹⁰ on the planar structure.

(2) The average phase velocity along the arms in the initial region was always that of the speed of light or greater indicating a fast wave progressing along the arm from tip to base. The phase velocity also tended to be a function of arm width in wavelengths.

Figure 18 is a composite curve of the relative amplitude curves shown in Figures 11 through 17, and Figure 19 is a composite curve of the relative phase curves. These two graphs were formed by referencing the initial amplitudes and phases such that the first regions of the curves were practically coincident. It must be admitted that this was rather arbitrary, but it did give an indication of the amount of energy which was being dissipated in the quasi dipole feed previously shown in Figure 5. Radiation from the feed section will be discussed later.

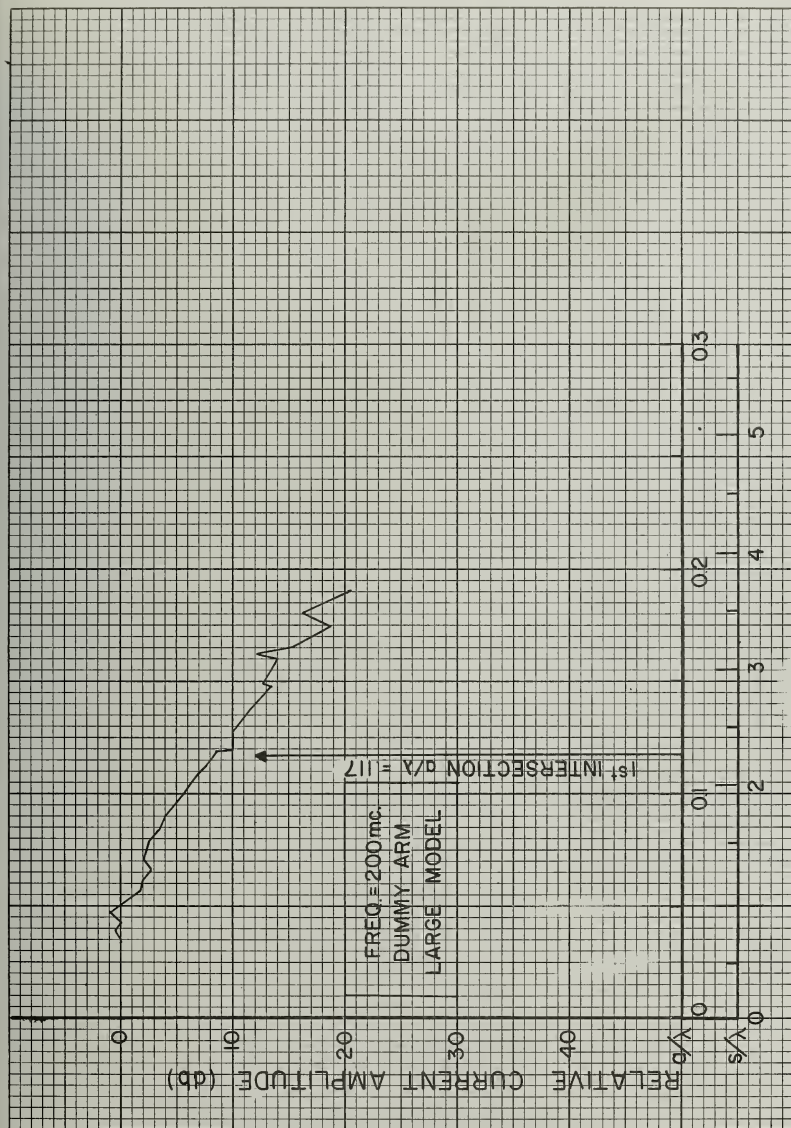


Figure 11. The current amplitude along the arm at 200 mc

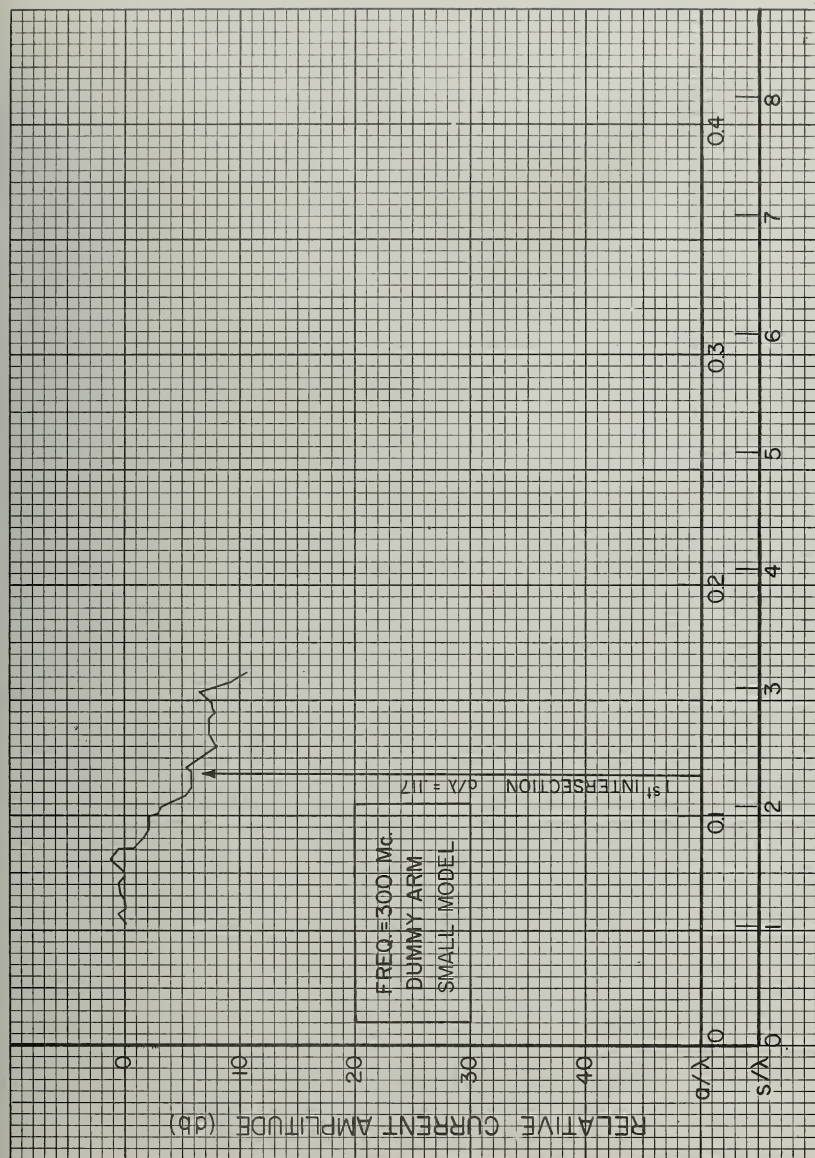


Figure 12. The current amplitude along the arm at 300 mc

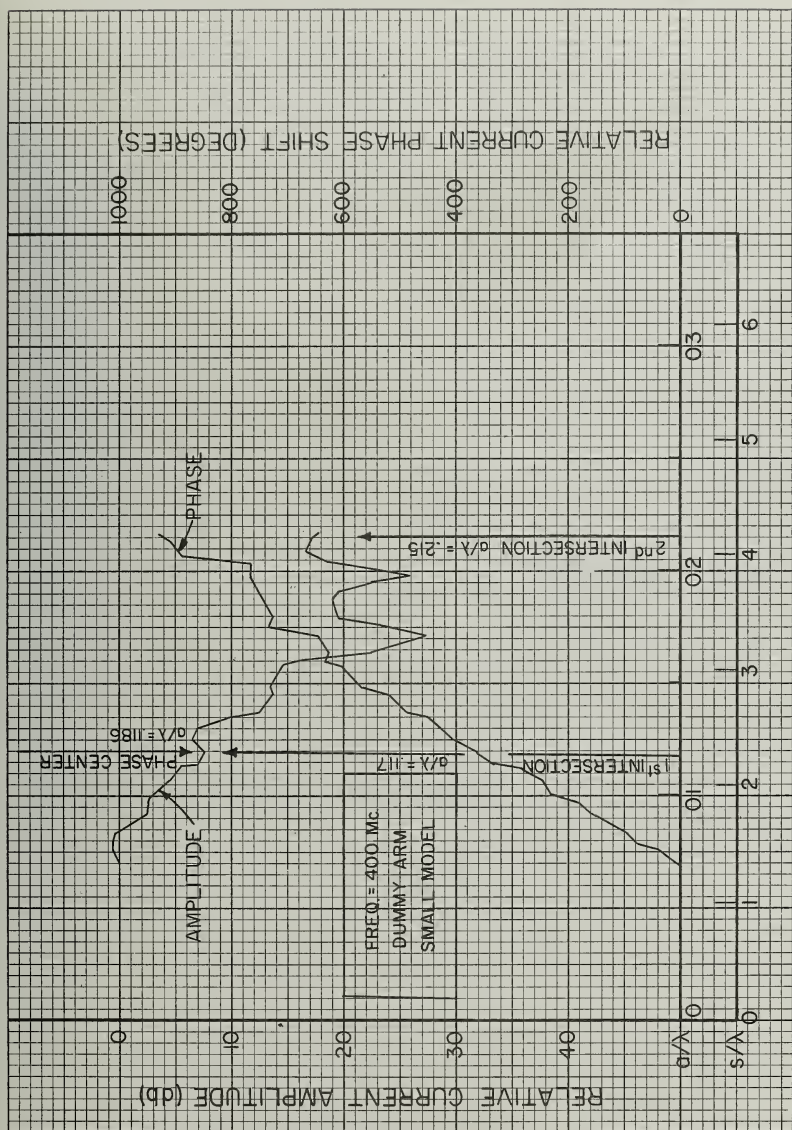


Figure 13. The current distribution along the arm at 400 mc

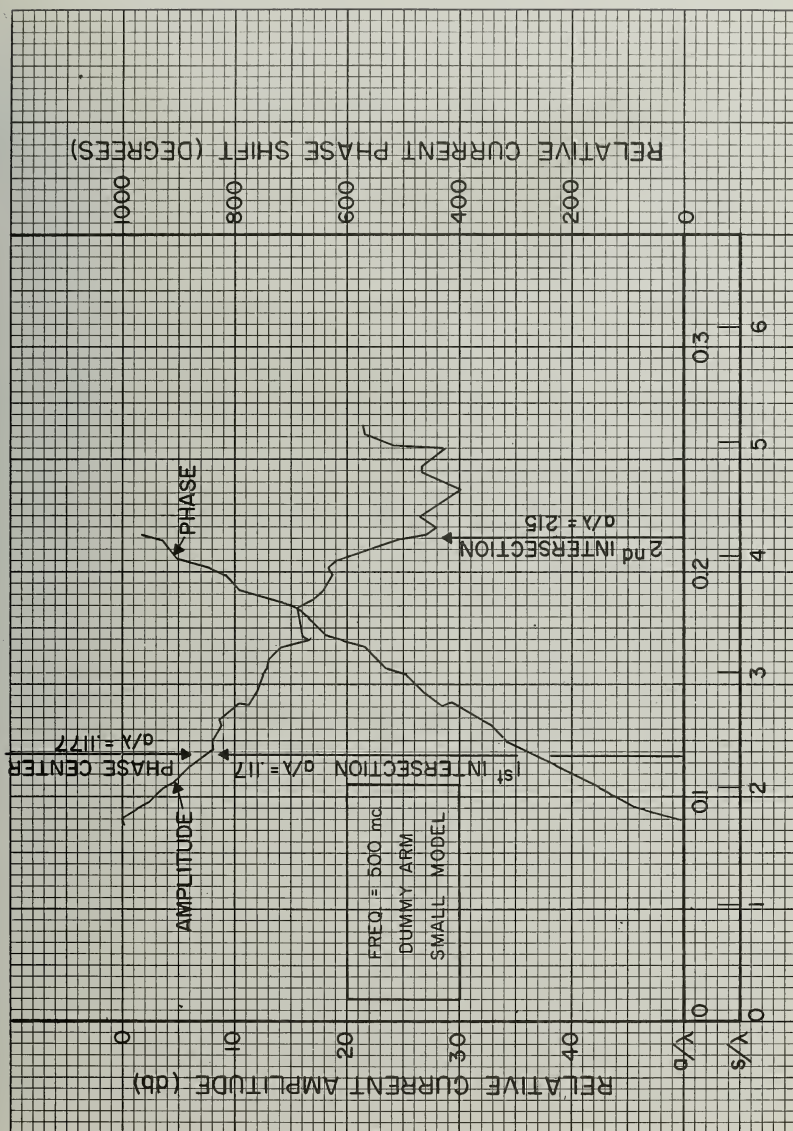


Figure 14. The current distribution along the arm at 500 mc

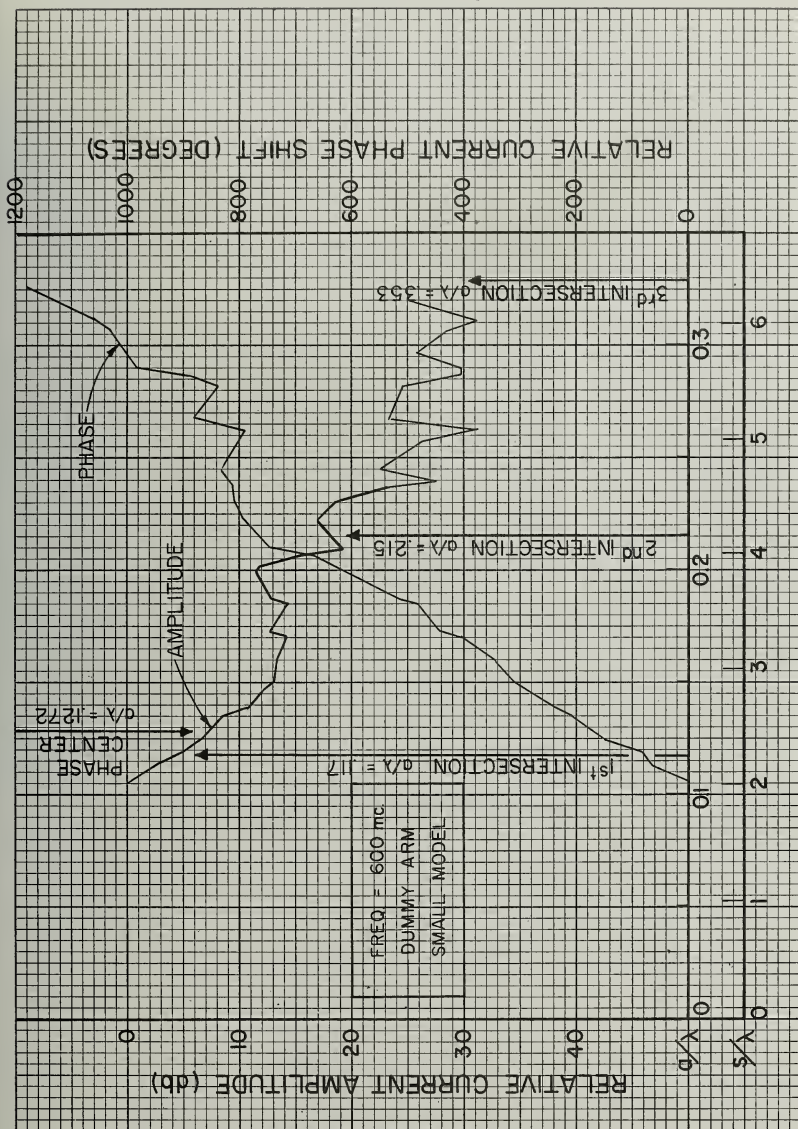


Figure 15. The current distribution along the arm at 600 mc

RELATIVE CURRENT PHASE SHIFT (DEGREES)

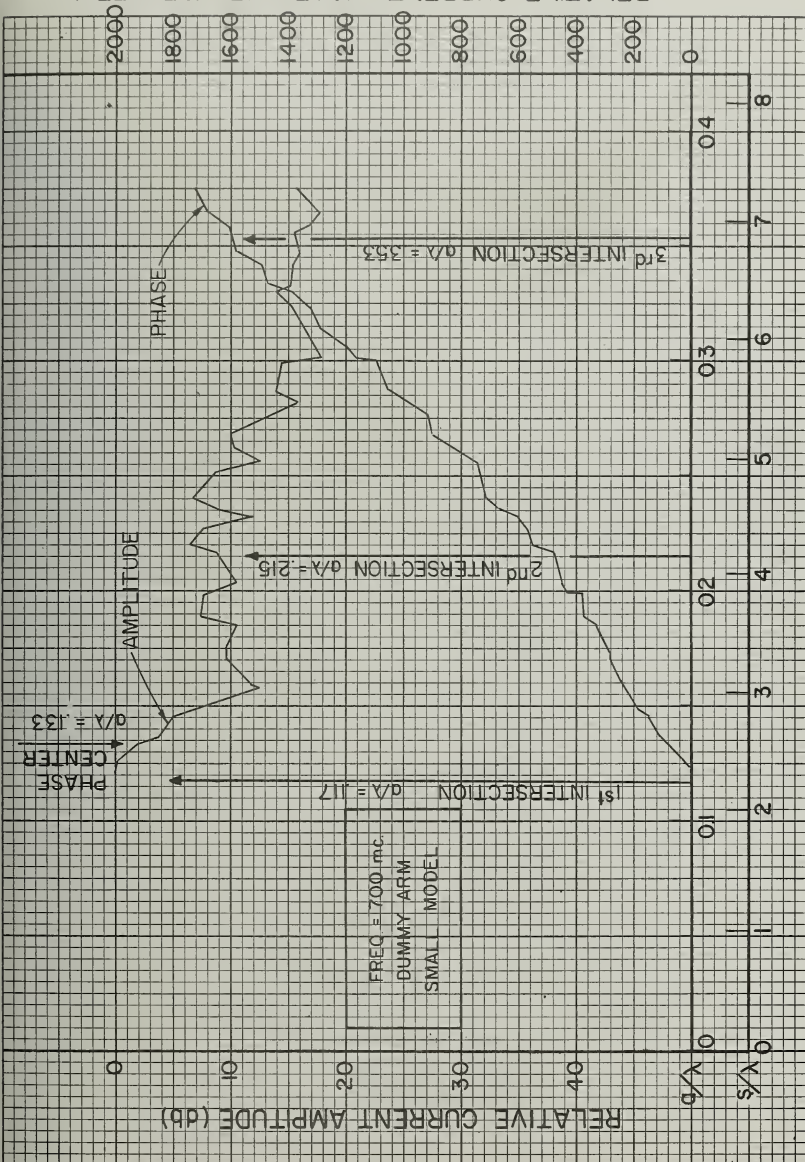


Figure 16. The current distribution along the arm at 700 mc

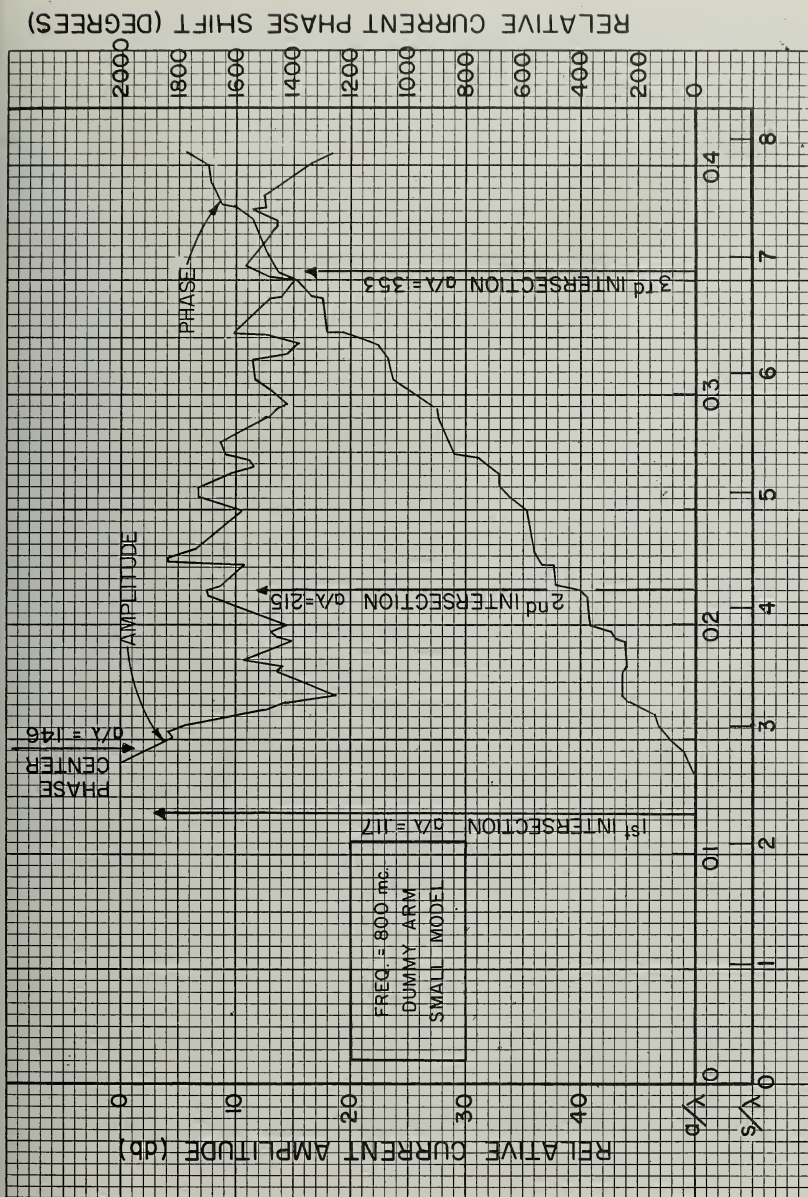


Figure 17. The current distribution along the arm at 800 mc

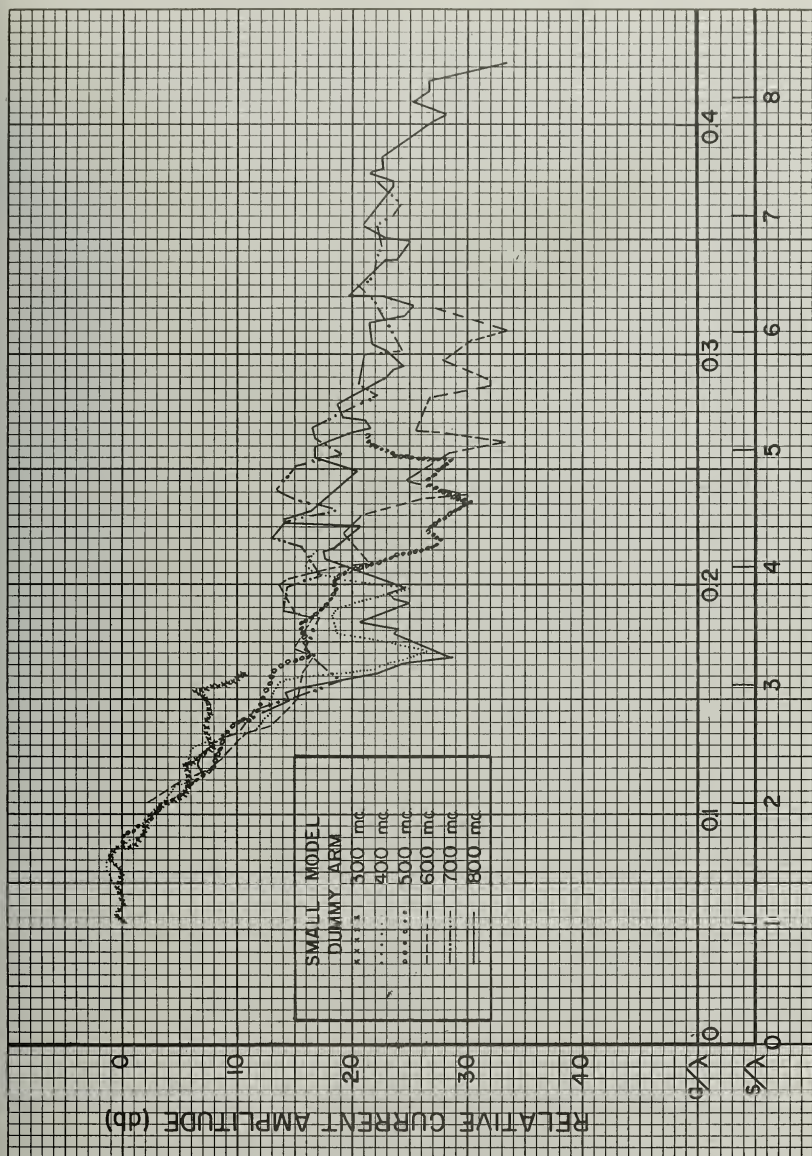


Figure 18. Composite curve of current amplitude along the arm as a function of frequency

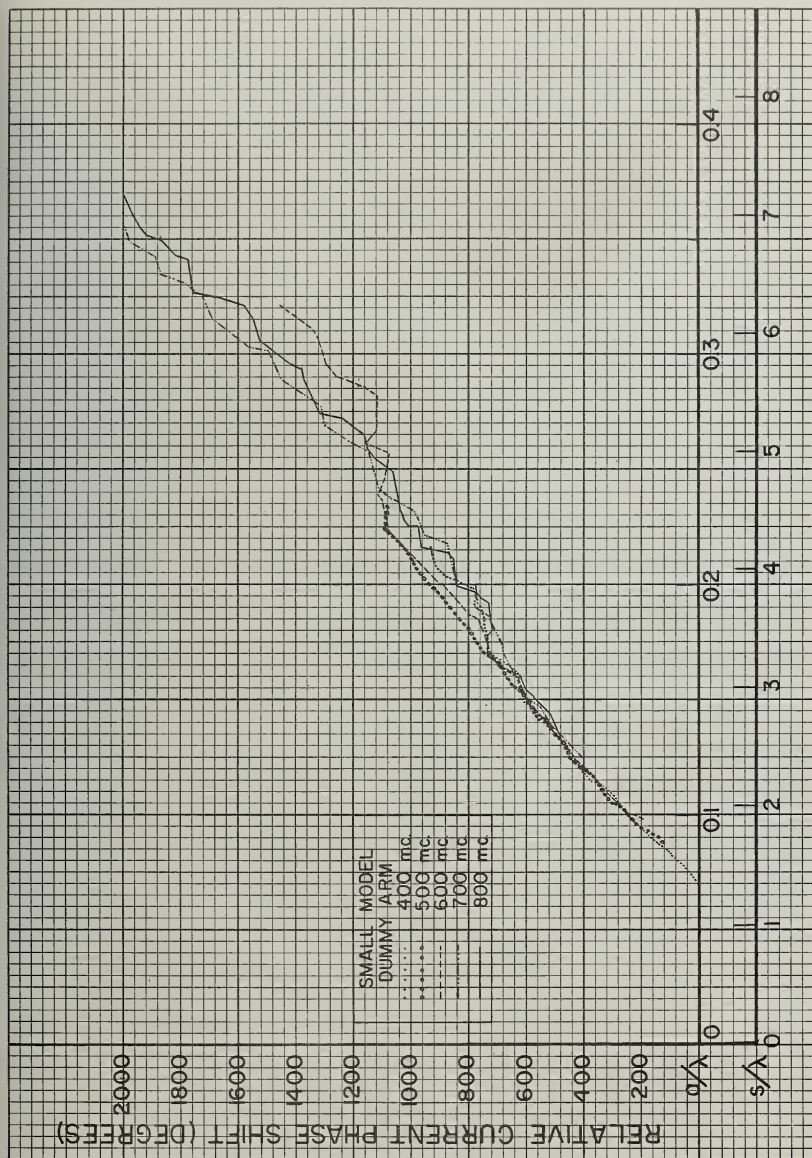


Figure 19. Composite curve of current phase shift along the arm as a function of frequency

In feeding the structure by the infinite balun method, it was evident that for operation at the lower frequencies the feed arm would have a different termination than the dummy arm. This gave a natural method to observe the base end effect on the current distribution at a low frequency. The relative magnitude was measured on both arms at 400 mc and is shown in Figure 20. The effects of the termination on the current distribution was rather obvious. It is interesting to note the rapidity with which the effect died out. This end effect is also demonstrated by comparing the data taken from both structures as was done in Figures 21, 22, and 23. In Figure 23, the end effect was not very evident, because both structures were, at 800 mc, rather large. The end effect at 800 mc was investigated by adding a $3/8\lambda$ extension to the dummy arm. It was felt that the small standing wave appearing in Figure 23 was not due to end effect as can be seen in Figure 24.

It was interesting to note, though, that the small standing wave had approximately the same period as the frequency of operation, i.e., half wave length nulls along the arm. Since this small standing wave was not due to a reflection, it was postulated that it was due to an interference between two different waves progressing in the same direction. This same phenomenon was observed by Marsh¹¹ when he measured the current distribution on a monofilar helical antenna. Marsh also demonstrated that a distribution similar to that shown in Figure 23 could be produced by a sum of four waves, two waves with different phase constants and their reflections. One of these waves had a phase constant equal to k , the phase constant of a free space wave, and the other had a phase constant approximately $1.4 k$. The wave traveling at the speed of light was attenuated while the other was not. As was stated previously

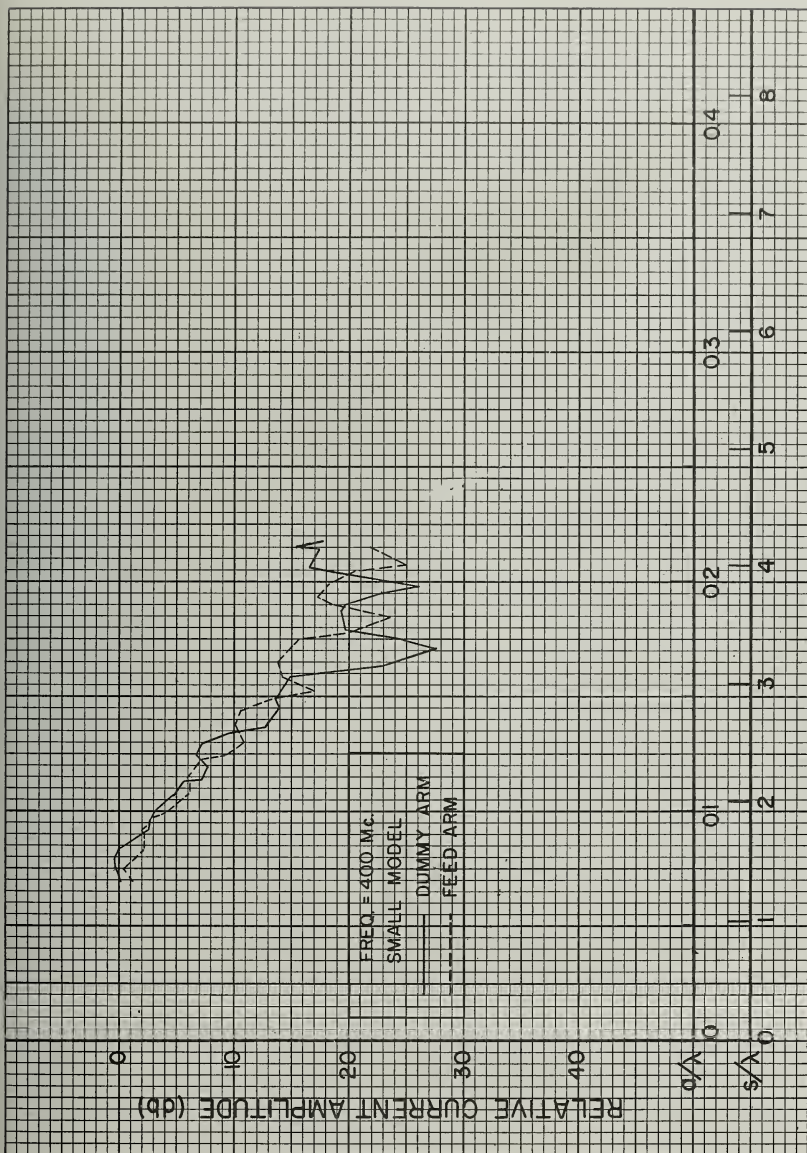


Figure 20. Comparison of current amplitude along both arms of the log-spiral at a low frequency

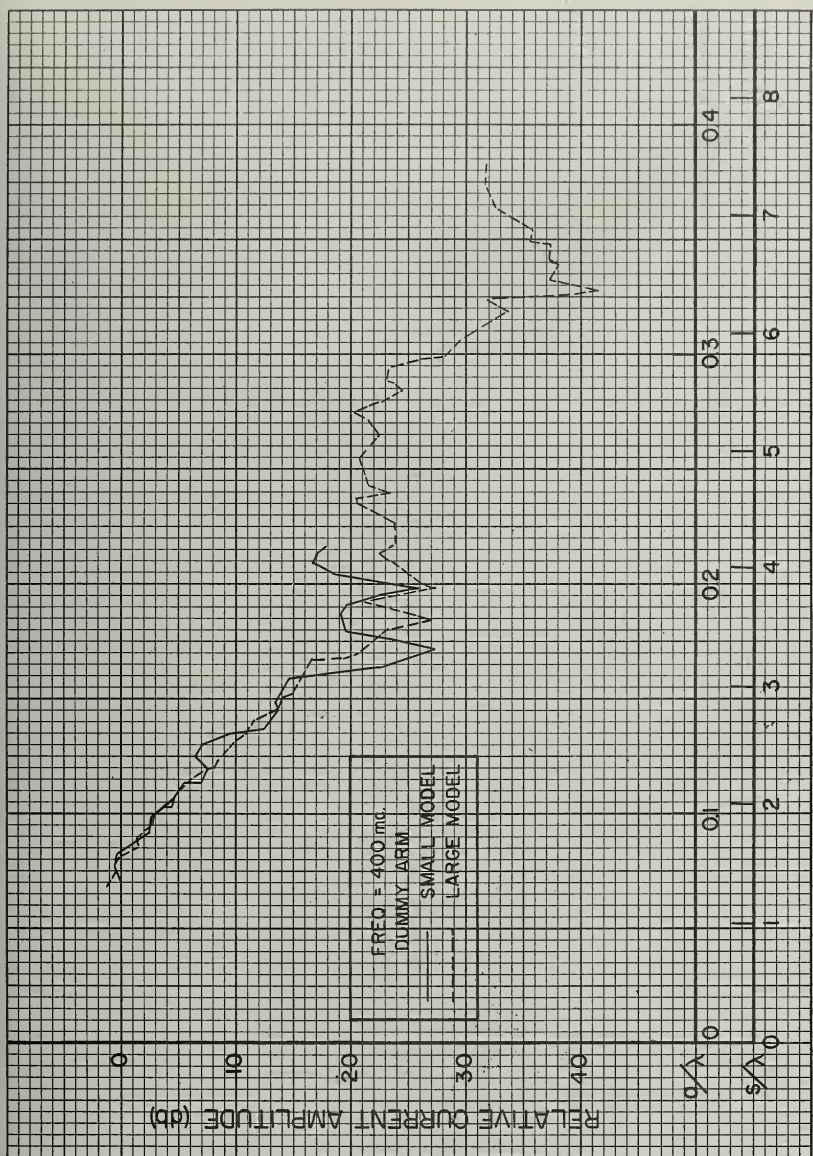


Figure 21. Comparison of the current amplitude along the dummy arms of both antennas at 400 mc

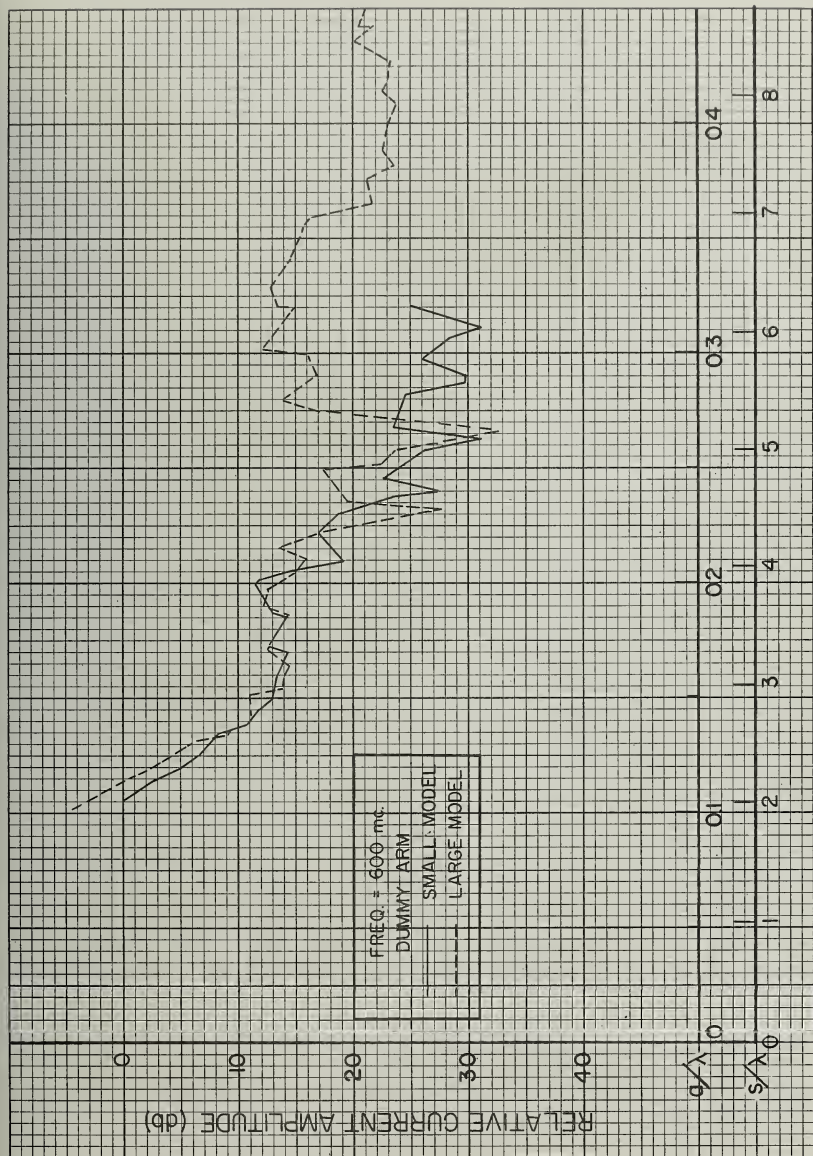


Figure 22. Comparison of the current amplitude along the dummy arms of both antennas at 600 mc

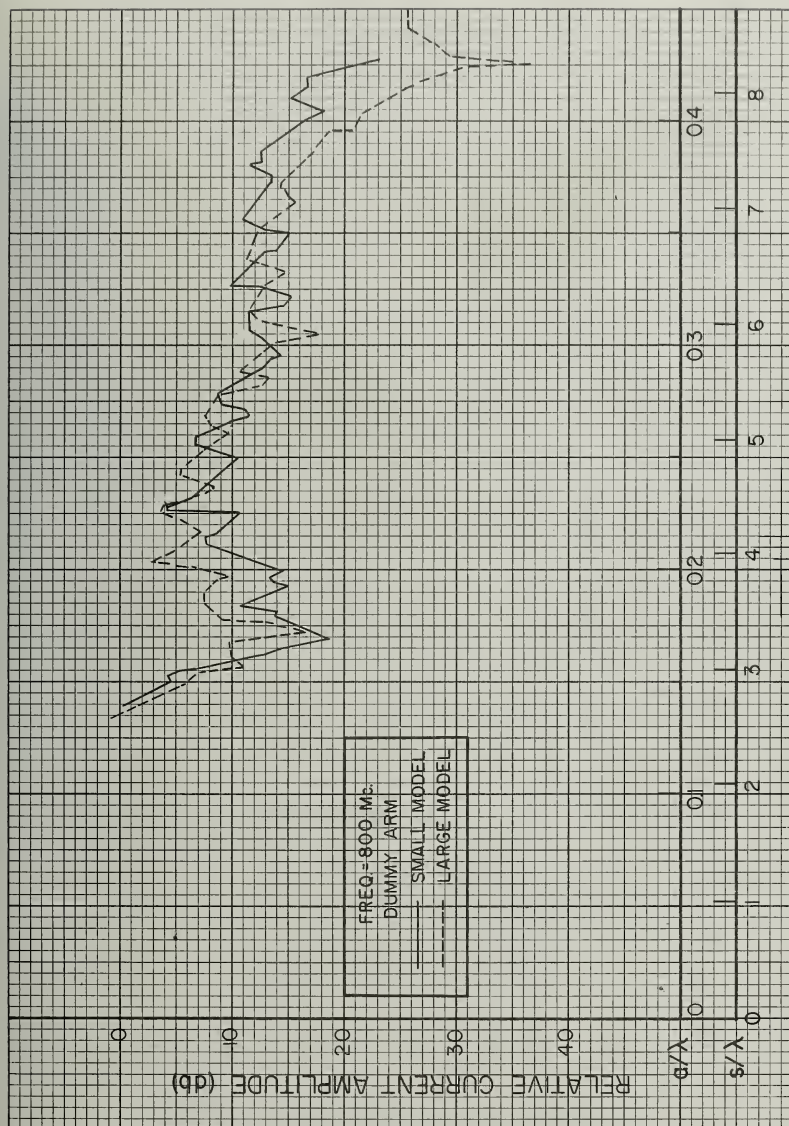


Figure 23. Comparison of the current amplitude along the dummy arms of both antennas at 800 mc

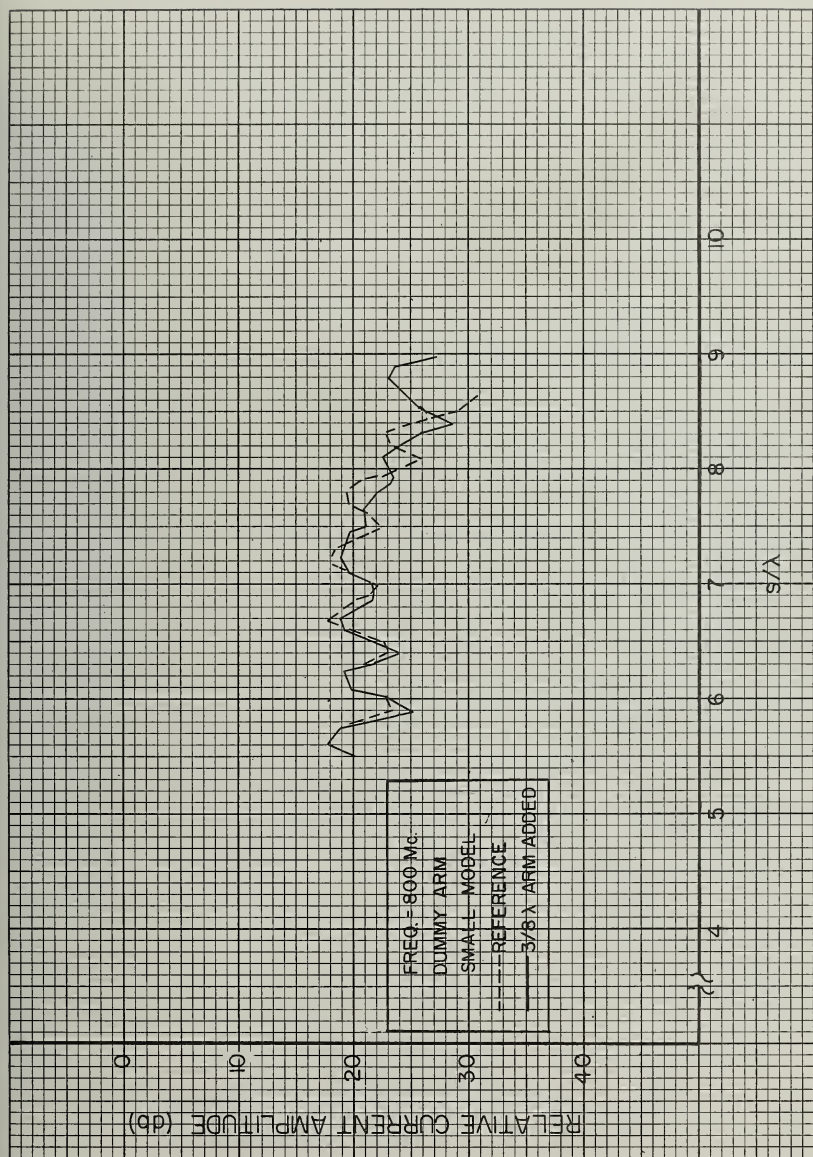


Figure 24. End effect at 800 mc on the small antenna

in Section 3, the fundamental wave had a phase constant approximately equal to k . The second wave could be explained as corresponding to a root following the $1 + ka/\cot \xi$ boundary line on the Brillouin diagram. By observing Figure 25, it is possible to see that at 800 mc the right hand root has an initial phase constant approximately $1.3 k$. Therefore, it was quite reasonable to assume that there were two waves traveling in the same direction and that the second was being excited with sufficient amplitude such that its effects on the distribution were no longer negligible. By assuming the existence of this second wave, it is possible to explain the general nature of the amplitude curves¹¹. It was felt that if only the fundamental wave, having a phase constant approximately equal to $2\pi/\lambda_0$, was present, that the amplitude curve would appear as in Figure 11. If the antenna was short enough in terms of wavelengths to allow reflections from the base, the fundamental wave and its reflection would yield a resultant as shown in Figure 13. If the two waves and small reflections from each were allowed, the distribution would appear as in Figures 14 through 17. By observing these five curves, it is possible to see the increasing effect of the second wave predicted by the $k-\beta$ diagram.

In Figure 25 the amplitude measured at 400 mc has been plotted with the $ka/\cot \xi$ axis as its abscissa. This plot gives an opportunity to observe the variation in the current amplitude and the variation in β , both as a function of ka . Also on this chart, the location of the tip truncation has been plotted along the $k = \beta$ line as a function of frequency. At these frequencies, no values of β could exist which were below and to the left of these marks since these values indicate the location of the excitation.

Figure 26 is an average curve taken from the two composite curves shown in Figures 18 and 19. In Figure 26, the locations of the first, second, and third

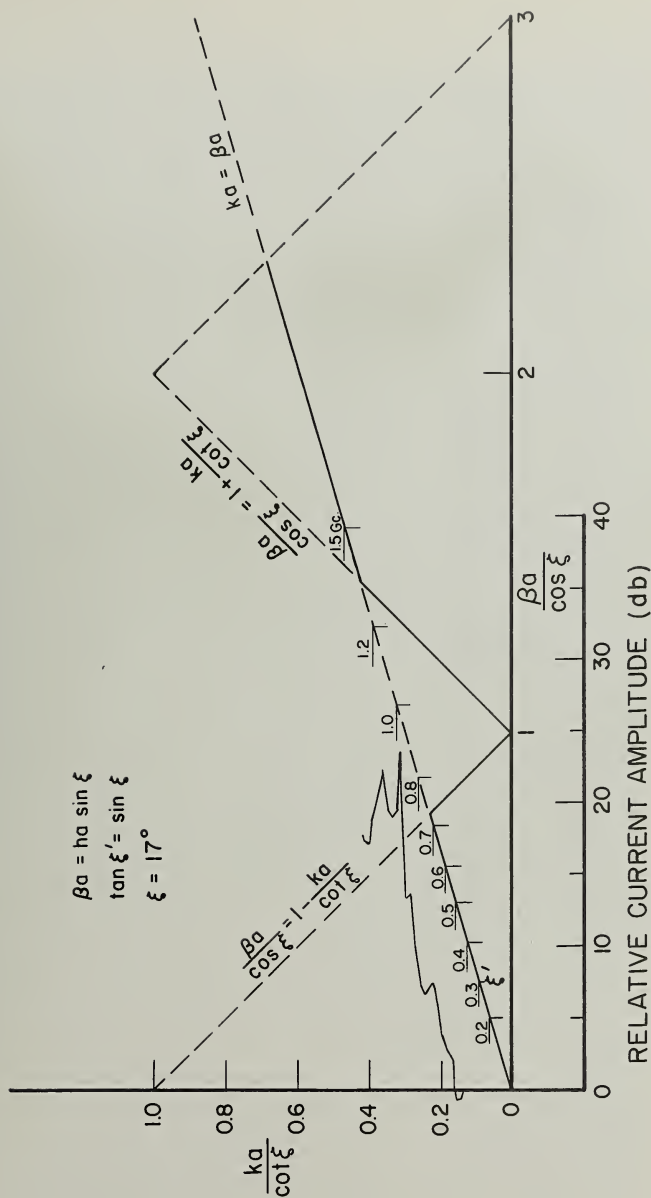


Figure 25. The current amplitude and location of the tip truncation superimposed on the k - β diagram

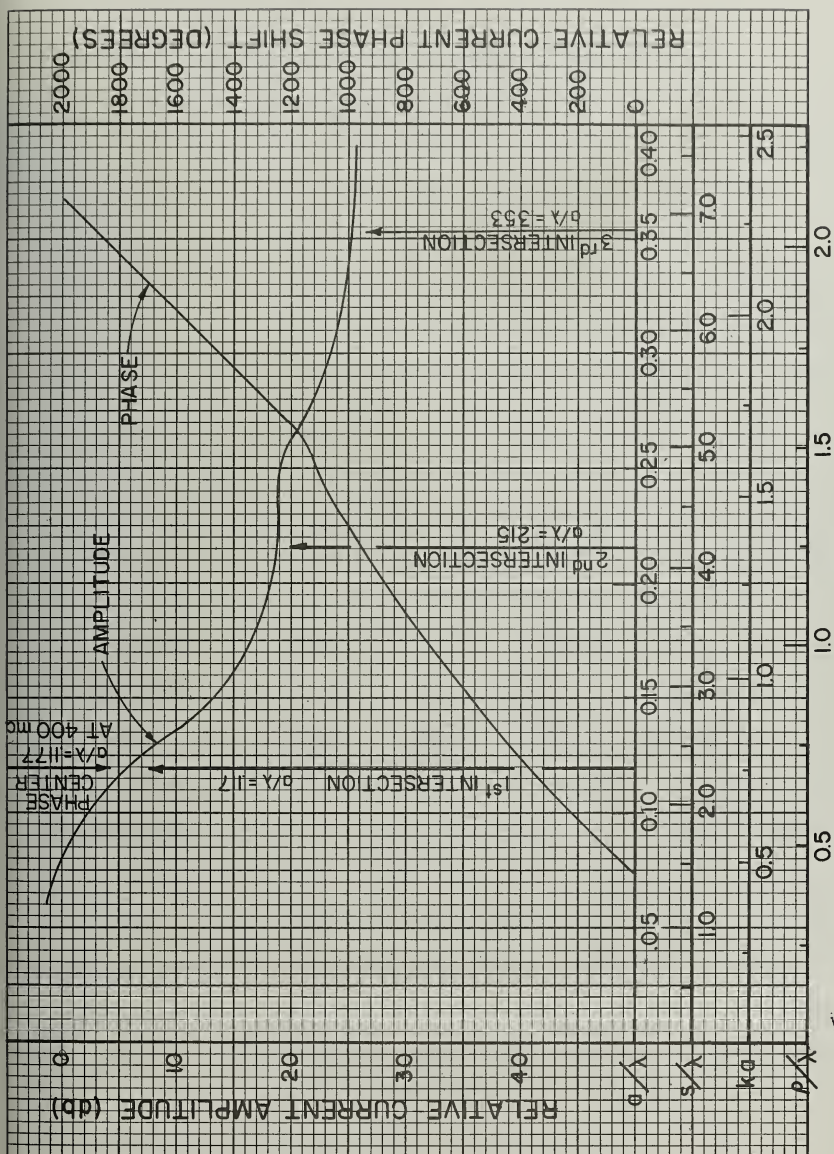


Figure 26. Average composite current distribution along the arm

intersections of the $k = \beta$ line and the boundary lines have been plotted. Also the location of the phase center measured at 400 mc has been plotted. It should be expected from observing Sensiper's work⁶, that the structure should have begun to radiate before the first intersection was reached. This radiation, due to the phase constant β being complex, should have continued beyond the second intersection. Somewhere between the second and third intersections the phase constant should have again become real meaning that the wave would only propagate along the arm until the radius expanded to correspond to the third intersection where the phase constant again becomes complex.

From observing Figure 26 there seems to be a good correlation between the regions where β is complex and the regions where the amplitude decays rapidly, possibly indicating the physical regions which contribute appreciably to the radiation. This correlation is also confirmed by the fact that the phase center appears approximately in the middle of the region which has the highest rate of amplitude decay. Dyson has shown that the phase centers for wire arm conical equiangular spiral antennas consistently lie in this region and has developed a quasi-empirical formula for the position of the phase center^{12,13}.

In order to confirm that this initial region of decay was the only one contributing appreciably to radiation it would be necessary to calculate the far field radiation pattern using only the current distribution over this initial region and compare this pattern to one calculated using the complete data.

6.2 Electric Field Radiation Patterns and SWR Measurements

The electric field radiation patterns and the SWR referred to 50 ohms have

been measured on the small model. This data appears in Figures 27, 28, and 29. It is interesting to note the frequency range where the SWR is essentially constant. This appears to be from approximately 350 mc to 500 mc. This was the same region where only the fundamental wave and its reflection existed as was indicated by the current distribution curves. This same region can be observed in the patterns, (note the broadening of the beamwidth above 600 mc). The lower frequency patterns are modified by reflections from the surroundings but they do not indicate any appreciable sidelobes. At frequencies above 800 mc, it was obvious that the quasi dipole feed was radiating appreciably. According to the $k-\beta$ diagram in Figure 25, at frequencies above 800 mc, the radiation should have been broadside, endfire, or a combination of these two. As can be seen, there was still a major lobe in the backfire direction. The most likely reason for this backward directed radiation was that the dipole feed section was radiating since it was greater than $3/8\lambda$ at these frequencies. The measured distance, from the apex of the cone to the phase center, in wavelengths has been shown in Figure 30. Superimposed upon this same chart is a plot of the distance, from the apex to the tip truncation, in terms of wavelengths. In order to have frequency independent operation, it is believed that the phase center should have remained essentially a constant distance, in wavelengths, from the apex. It can be seen though, that the tip truncation was influencing the location of the phase center as low as 600 mc¹². Again this is approximately the same frequency at which the rest of the data began to deviate from that which one might associate with normal operation, i.e., one attenuated wave traveling approximately at the speed of light from the feed along the arm toward the base.

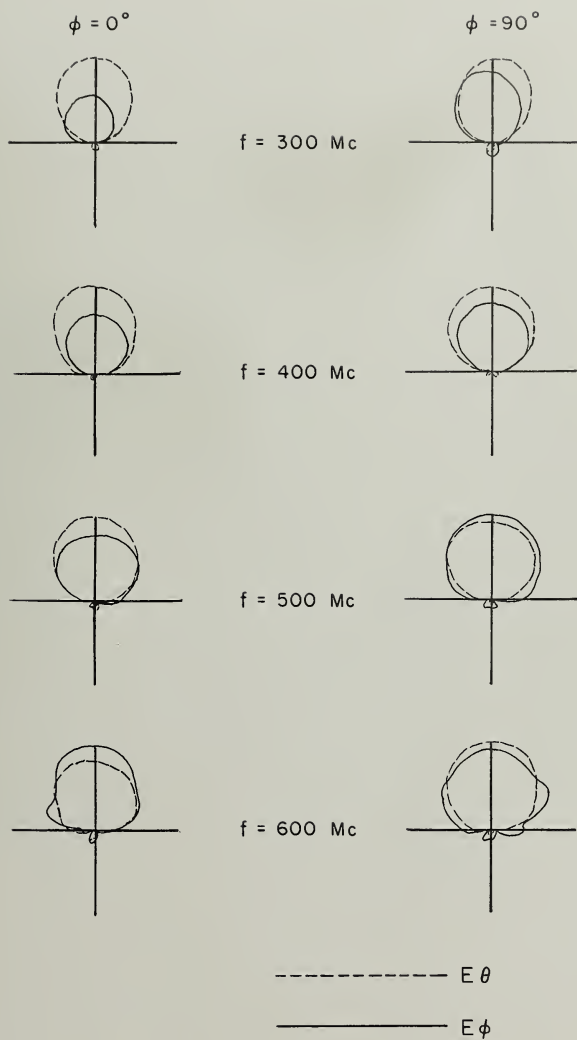


Figure 27. Electric field radiation patterns of the small antenna

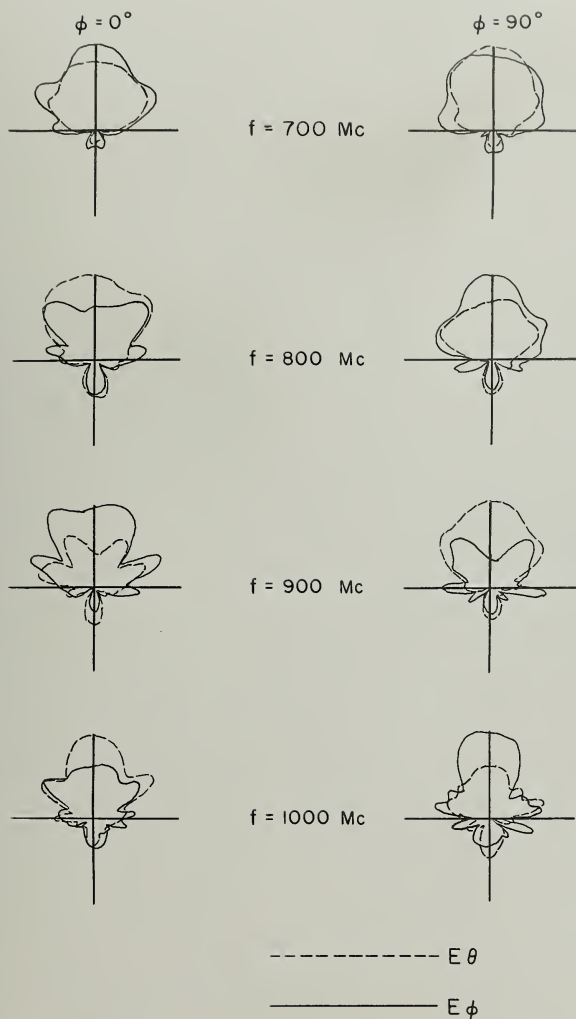


Figure 28. Electric field radiation patterns of the small antenna

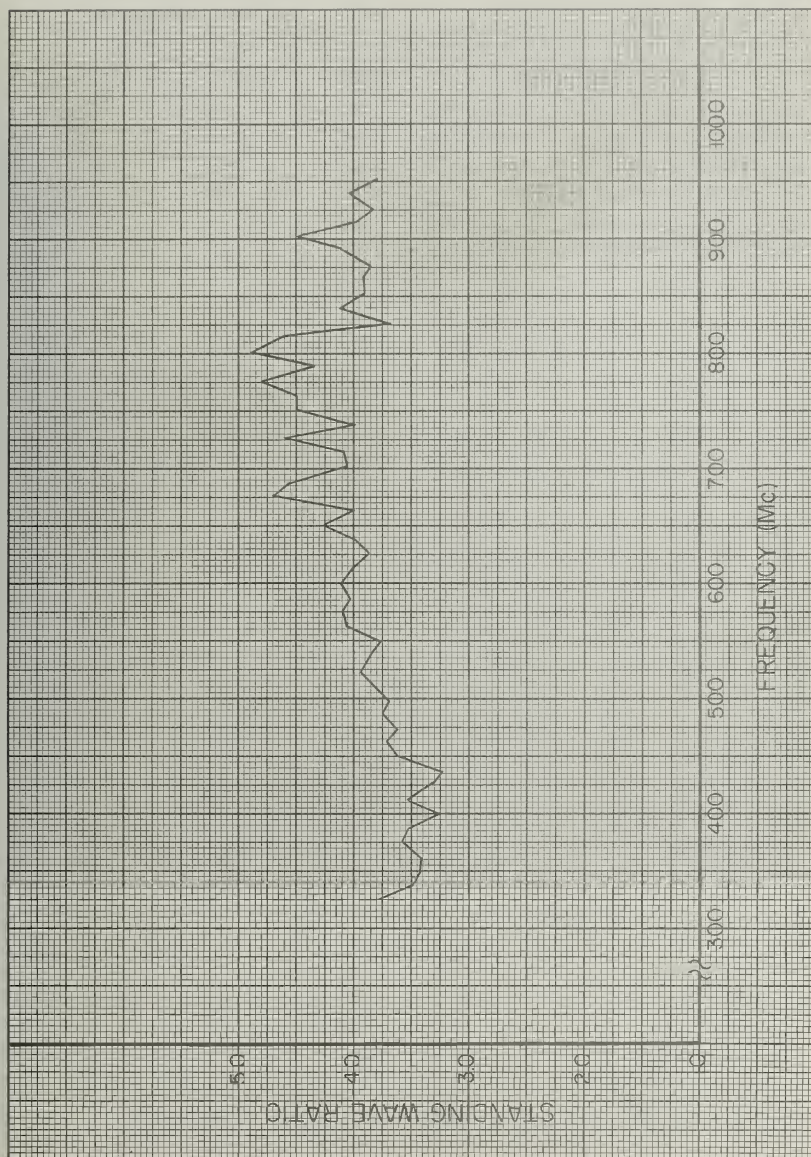


Figure 29. Standing wave ratio referred to 50 Ω as a function of frequency

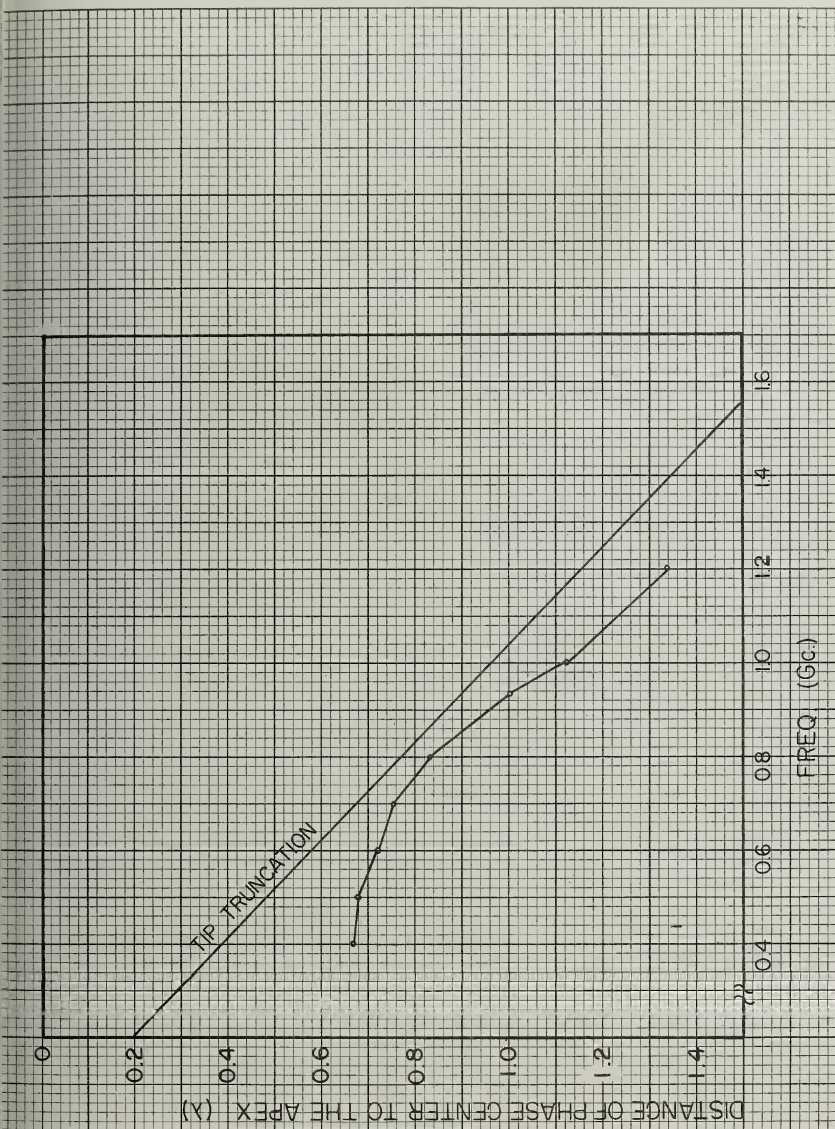


Figure 30. Relative distances of the phase center and tip truncation to the apex as a function of frequency

7. CONCLUSION

It was the purpose of these investigations to lead to a better understanding of the operation of the conical equiangular spiral antenna. The investigation was conducted by measuring the current distribution below, throughout, and above the normal frequency independent operating range. The phase center, far field patterns, and standing wave ratio were also measured. The results confirm the possibility of applying the general theory of backward wave radiation from periodic structures to the analysis of the radiation characteristics of the conical log-spiral antenna.

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